## Department of Mathematics

## 2019 - Spring Semester

(Disclaimer: Be advised that some information on this page may not be current due to course scheduling changes. Please view either the UH Class Schedule page or your Class schedule in myUH for the most current/updated information.)

## GRADUATE COURSES - SPRING 2019

This schedule is subject to changes. Please contact the Course Instructor for confirmation.

| Course | $\begin{aligned} & \text { Class } \\ & \text { \# } \end{aligned}$ | Course Title | Course Day \& Time | Rm \# | Instructor |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Math 4309 | 6259 | Mathematical Biology | MW, 2:30-4:00PM | SEC 104 | R. Azevedo |
| Math 4315 | 12147 | Graph Theory w/Applications | TuTh, 4:00-5:30PM | SEC 202 | K. Josic |
| Math 4332/6313 | 2895 | Introduction to Real Analysis II | TuTh, 2:30-4:00PM | AH 301 | M. Kalantar |
| Math 4351 | 13920 | Differential Geometry II | TuTh, 1:00-2:30PM | SEC 203 | M. Ru |
| Math 4362 | 13921 | Theory of Differential Equations and Nonlinear Dynamics | TuTh, 4:00-5:30PM | AH 302 | W. Ott |
| Math 4364 | 9310 | Intro. to Numerical Analysis in Scientific Computing | MW, 4:00-5:30PM | $\begin{aligned} & \text { D2 } \\ & \text { LECT2 } \end{aligned}$ | T.W. Pan |
| Math 4364 | 17945 | Intro. to Numerical Analysis in Scientific Computing | Online | Online | J. Morgan |
| Math 4365 | 7697 | Numerical Methods for Differential Equations | TuTh, 11:30AM1PM | CBB 120 | J. He |
| Math 4377/6308 | 5199 | Advanced Linear Algebra I | MWF, Noon-1:00PM | SEC 103 | D. Wagner |
| Math 4378/6309 | 2896 | Advanced Linear Algebra II | TuTh, 11:30AM1PM | F 154 | A. Mamonov |
| Math 4380 | 2897 | A Mathematical Introduction to Options | MW, 1-2:30PM | SEC 105 | I. Timofeyev |
| Math 4389 | 2898 | Survey of Undergraduate Mathematics | MWF, Noon-1PM | SEC 205 | M. Almus |

## GRADUATE ONLINE COURSES

| Course | Class \# | Course Title | Course Day \& Time | Instructor |
| :--- | :--- | :--- | :--- | :--- |
| Math 5330 | 4255 | Abstract Algebra | Arrange (online course) | K. Kaiser |
| Math 5332 | 2917 | Differential Equations | Arrange (online course) | G. Etgen |
| Math 5334 | 13922 | Complex Analysis | Arrange (online course) | S. Ji |
| Math 5344 | 18243 | Introduction to Scientific Computing | Arrange (online course) | J. Morgan |
| Math 5386 | 5938 | Regression and Linear Models | Arrange (online course) | C. Peters |

GRADUATE COURSES

| Course | Class \# | Course Title | Course Day \& Time | Rm \# | Instructor |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Math 6303 | 2924 | Modern Algebra II | MW, 1-2:30pm | C 105 | G. Heier |
| Math 6308 | 4421 | Advanced Linear Algebra I | MWF, Noon-1pm | SEC 103 | D. Wagner |
| Math 6308 | 8599 | Advanced Linear Algebra I (online) | Online | Online | TBA |
| Math 6309 | 4429 | Advanced Linear Algebra II | TuTh, 11:30am-1pm | F 154 | A. Mamonov |
| Math 6313 | 4420 | Introduction to Real Analysis | TuTh, 2:30-4pm | C 106 | M. Kalantar |
| Math 6321 | 2941 | Theory of Functions of a Real Variable | MWF, 11am-Noon | AH 108 | M. Tomforde |
| Math 6323 | 13923 | Functional Complex Variable | MWF, 9-10am | AH 301 | S. Ji |
| Math 6361 | 4424 | Applicable Analysis | MWF, 10-11am | AH 301 | B. Bodmann |
| Math 6365 | 12154 | Automatic Learning and Data Mining | TuTh, 11:30am-1pm | CBB 124 | R. Azencott |
| Math 6367 | 2942 | Optimization Theory | MW, 4-5:30pm | SEC 206 | R. Hoppe |
| Math 6371 | 2943 | Numerical Analysis | MW, 1-2:30pm | AH 303 | Y. Kuznetsov |
| Math 6383 | 2944 | Probability Statistics | TuTh, 4-5:30pm | AH 7 | W. Fu |
| Math 6385 | 12153 | Continuous-Time Models in Finance | TuTh, 2:30-4pm | F 162 | E. Kao |
| Math 6397 | 13924 | Sobolev Calculus \& Sobolev Spaces | TuTh, 1-2:30pm | AH 203 | G. Auchmuty |
| Math 6397 | 13925 | Time Series Analysis | TuTh, 10-11:30am | AH 203 | E. Kao |
| Math 7321 | 13926 | Functional Analysis | MWF, Noon-1pm | AH 301 | D. Blecher |
| Math 7350 | 13927 | Geometry of Manifolds | TuTh, 11:30am-1pm | SW 423 | A. Török |
| Math 7394 | 13929 | Ergodic Theory \& Thermodynamic Formalism | MWF, 11am-Noon | AH 2 | V. Climenhaga |
| Math 7396 | 13930 | Multigrid Methods | MW, 4-5:30pm | AH 301 | M. Olshanskiy |

## SENIOR UNDERGRADUATE COURSES

## Math 4309 (6259) - Mathematical Biology

Prerequisites: MATH 3331 and BIOL 3306 or consent of instructor

Text(s):

Description:
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Prerequisites:

Text(s):

Description:

## Math 4315 (12147) - Graph Theory w/Applications

Either MATH 3330 or MATH 3336 and three additional hours of 3000-4000 level Mathematics Networks, Crowds, and Markets: Reasoning About a Highly Connected World. By David Easley and Jon Kleinberg. This text is availabe at this link:
https://www.cs.cornell.edu/home/kleinber/networks-book/
Introduction to basic concepts, results, methods, and applications of graph theory.
Additional Description: How does information propagate between friends and acquaintances on social media? How do diseases spread, and when do epidemics start? How should we design power grids to avoid failures, and systems of roads to optimize traffic flow? These questions can be addressed using network theory. Students in the course will develop a sound knowledge of the basics of graph theory, as well as some of the computational tools used to address the questions above. Course topics include basic structural features of networks, generative models of networks, centrality, random graphs, clustering, and dynamical processes on graphs.

Math 4332 (2895) - Introduction to Real Analysis II

Prerequisites:
Text(s):

Description:

MATH 4331 or consent of instructor
Real Analysis with Real Applications | Edition: 1; Allan P. Donsig, Allan P. Donsig; ISBN: 9780130416476

Further development and applications of concepts from MATH 4331. Topics may vary depending on the instructor's choice. Possibilities include: Fourier series, point-set topology, measure theory, function spaces, and/or dynamical systems.

Prerequisites:
Text(s):

Description:
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## Math 4362 (13921) - Theory of Differential Equations an Nonlinear Dynamics

Prerequisites:
Text(s):

Description:

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Text(s):

Description:
MATH 4350.
Instructor's notes will be provided.
Continuation of the study of Differential Geometry from MATH 4350. Holonomy and the GaussBonnet theorem, introduction to hyperbolic geometry, surface theory with differential forms, calculus of variations and surfaces of constant mean curvature, abstract surfaces (2D Riemannian manifolds).

MATH 3331, or equivalent, and three additional hours of 3000-4000 level Mathematics. Nonlinear Dynamics and Chaos (2nd Ed.) by Strogatz. ISBN: 978-0813349107

ODEs as models for systems in biology, physics, and elsewhere; existence and uniqueness of solutions; linear theory; stability of solutions; bifurcations in parameter space; applications to oscillators and classical mechanics.

Math 4364 (9310)- Numerical Analysis in Scientific Computing
MATH 3331 and COSC 1410 or equivalent or consent of instructor.

## Instructor's Prerequisite Notes:

Prerequisites:

1. MATH 2331, In depth knowledge of Math 3331 (Differential Equations) or Math 3321 (Engineering Mathematics)
2. Ability to do computer assignments in FORTRAN, C, Matlab, Pascal, Mathematica or Maple.

Numerical Analysis (9th edition), by R.L. Burden and J.D. Faires, Brooks-Cole Publishers, ISBN:9780538733519

This is an one semester course which introduces core areas of numerical analysis and scientific computing along with basic themes such as solving nonlinear equations, interpolation and splines fitting, curve fitting, numerical differentiation and integration, initial value problems of ordinary
<< back to top >> differential equations, direct methods for solving linear systems of equations, and finite-difference approximation to a two-points boundary value problem. This is an introductory course and will be a mix of mathematics and computing.

MATH 3331 and COSC 1410 or equivalent or consent of instructor.

## Instructor's Prerequisite Notes:

| Prerequisites: | 1. MATH 2331, In depth knowledge of Math 3331 (Differential Equations) or Math 3321 (Engineering <br> Mathematics) |
| :--- | :--- |
|  | 2. Ability to do computer assignments in FORTRAN, C, Matlab, Pascal, Mathematica or Maple. |
| Text(s): | Numerical Analysis (9th edition), by R.L. Burden and J.D. Faires, Brooks-Cole Publishers, <br> ISBN:9780538733519 |

This is an one semester course which introduces core areas of numerical analysis and scientific computing along with basic themes such as solving nonlinear equations, interpolation and splines fitting, curve fitting, numerical differentiation and integration, initial value problems of ordinary differential equations, direct methods for solving linear systems of equations, and finite-difference approximation to a two-points boundary value problem. This is an introductory course and will be a mix of mathematics and computing.

Math 4365 (7397) - Numerical Methods for Differential Equations
Description: MATH 3331, or equivalent, and three additional hours of 3000-4000 level Mathematics. TITLE:TBA, AUTHOR:TBA, ISBN:TBA
Numerical differentiation and integration, multi-step and Runge-Kutta methods for ODEs, finite difference and finite element methods for PDEs, iterative methods for linear algebraic systems and eigenvalue computation.

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Prerequisites:
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Prerequisites:
Text(s):
Math 4377 (5199) - Advanced Linear Algebra I
MATH 2331 or equivalent, and three additional hours of 3000-4000 level Mathematics. Linear Algebra | Edition: 4; Stephen H. Friedberg, Arnold J. Insel, Lawrence E. Spence; ISBN: 9780130084514

Linear systems of equations, matrices, determinants, vector spaces and linear transformations, eigenvalues and eigenvectors.

Additional Notes: This is a proof-based course. It will cover Chapters 1-4 and the first two sections of Chapter 5. Topics include systems of linear equations, vector spaces and linear transformations (developed axiomatically), matrices, determinants, eigenvectors and diagonalization.

Math 4378 (2896) - Advanced Linear Algebra II
MATH 4377
Linear Algebra, Fourth Edition, by S.H. Friedberg, A.J Insel, L.E. Spence,Prentice Hall, ISBN 0-13-008451-4; 9780130084514

Similarity of matrices, diagonalization, Hermitian and positive definite matrices, normal matrices, and canonical forms, with applications.

Instructor's Additional notes: This is the second semester of Advanced Linear Algebra. I plan to cover Chapters 5, 6, and 7 of textbook. These chapters cover Eigenvalues, Eigenvectors, Diagonalization, Cayley-Hamilton Theorem, Inner Product spaces, Gram-Schmidt, Normal Operators (in finite dimensions), Unitary and Orthogonal operators, the Singular Value Decomposition, Bilinear and Quadratic forms, Special Relativity (optional), Jordan Canonical form.

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Prerequisites:
Text(s):

Description:
Math 4380 (2897) - A Mathematical Introduction to Options
MATH 2433 and MATH 3338.
An Introduction to Financial Option Valuation: Mathematics, Stochastics and Computation | Edition: 1; Desmond Higham; 9780521547574
Arbitrage-free pricing, stock price dynamics, call-put parity, Black-Scholes formula, hedging, pricing of European and American options.

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Prerequisites:

Text(s):

Description:
Math 4389 (2898) - Survey of Undergraduate Mathematics
MATH 3330, MATH 3331, MATH 3333, and three hours of 4000-level Mathematics. Instructor will use his own notes
A review of some of the most important topics in the undergraduate mathematics curriculum.

> Math 4397 (14519) - Statistical \& Machine Learning Catalog Prerequisite: MATH 3333 or approval of the instructor. Instructor Prerequisite: MATH 3339
> While lecture notes will serve as the main source of material for the course, the following book constitutes a great reference: "An Introduction to Statistical Learning (with applications in R)" by James, Witten et al.
> Instructor's Description: Course will deal with applications for such statistical learning techniques as maximal margin classifiers, support vector machines, K-means and hierarchical clustering. Other topics might include: algorithm performance evaluation, cluster validation, data scaling, resampling methods. R Statistical programming will be used throughout the course.

Software: Make sure to download R and RStudio (which can't be installed without R ) before the course starts. Use the link https://www.rstudio.com/products/rstudio/download/ to download it from the mirror appropriate for your platform. Let me know via email in case you encounter difficulties.

## ONLINE GRADUATE COURSES

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## MATH 5330 (4255) - Abstract Algebra

Prerequisites:

Text(s):

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Prerequisites:
Text(s):

Description:

Prerequisites:
Text(s):

Description:

Graduate standing,

Abstract Algebra, A First Course by Dan Saracino. Waveland Press, Inc. ISBN 0-88133-665-3 (You can use the first edition. The second edition contains additional chapters that cannot be covered in this course.)

Groups, rings and fields; algebra of polynomials, Euclidean rings and principal ideal domains. Does not apply toward the Master of Science in Mathematics or Applied Mathematics.

Other Notes: This course is meant for students who wish to pursue a Master of Arts in Mathematics (MAM). Please contact me in order to find out whether this course is suitable for you and/or your degree plan. Notice that this course cannot be used for MATH 3330, Abstract Algebra.

MATH 5332 (2917) - Differential Equations
Graduate standing. MATH 5331.
TBA

Linear and nonlinear systems of ordinary differential equations; existence, uniqueness and stability of solutions; initial value problems; higher dimensional systems; Laplace transforms. Theory and applications illustrated by computer assignments and projects. Applies toward the Master of Arts in Mathematics degree; does not apply toward the Master of Science in Mathematics or the Master of Science in Applied Mathematics degrees.

## MATH 5334 (13922) - Complex Analysis

Graduate standing: and two semesters of calculus. The course will be based on my notes.

This course is an introduction to complex analysis. It will cover the theory of holomorphic functions, Cauchy theorem and Cauchy integral formula, residue theorem, harmonic and subharmonic functions, and other topics.

On-line course is taught through Blackboard Learn, visit http://www.uh.edu/webct/ for information on obtaining ID and password.

In each week, some lecture notes will be posted in Blackboard Learn, including homework assignment.

Homework will be turned in by the required date through Blackboard Learn. It must be in pdf file. There are two exams. Homework and test problems are mostly computational in nature.

## Text(s):

Description:

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Prerequisites:

Text(s):

Description:
MATH 5386 (5938) - Regression and Linear Models (VEE approved course)
Graduate standing. Two semesters of calculus, one semester of linear algebra, and MATH 5385, or consent of instructor. Introduction to Linear Regression Analysis | Edition:5; Montgomery, Peck, Vining; ISBN: 9780470542811; Wiley

Simple and multiple linear regression, linear models, inferences from the normal error model, regression diagnostics and robust regression, computing assignments with appropriate software. Applies toward Master of Arts in Mathematics degree; does not apply toward the Master of Science in Mathematics or the Master of Science in Applied Mathematics degrees.

Note: This course is VEE approved for the regression component only. Approval Code: 4458-11008. For more information on VEE approved courses, click here.

## GRADUATE COURSES

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MATH 6303 (2924) - Modern Algebra II

Graduate standing: MATH 4333 or MATH 4378

Prerequisites:

Text(s):

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Prerequisites:

Text(s):

Description:

Additional Prerequisites: students should be comfortable with basic measure theory, groups rings and fields, and point-set topology

No textbook is required.

Topics from the theory of groups, rings, fields, and modules.

Additional Description: This is primarily a course about analysis on topological groups. The aim is to explain how many of the techniques from classical and harmonic analysis can be extended to the setting of locally compact groups (i.e. groups possessing a locally compact topology which is compatible with their algebraic structure). In the first part of the course we will review basic point set topology and introduce the concept of a topological group. The examples of $p$-adic numbers and the Adeles will be presented in detail, and we will also spend some time discussing SL_2(R). Next we will talk about characters on topological groups, Pontryagin duality, Haar measure, the Fourier transform, and the inversion formula. We will focus on developing details in specific groups (including those mentioned above), and applications to ergodic theory and to number theory will be discussed.

## MATH 6308 (4421) - Advanced Linear Algebra I

Graduate standing: MATH 2331 and a minimum of 3 semester hours transformations, eigenvalues and eigenvectors.
Linear Algebra | Edition: 4; Stephen H. Friedberg, Arnold J. Insel, Lawrence E. Spence; ISBN: 9780130084514

Transformations, eigenvalues and eigenvectors.

Additional Notes: This is a proof-based course. It will cover Chapters 1-4 and the first two sections of Chapter 5. Topics include systems of linear equations, vector spaces and linear transformations (developed axiomatically), matrices, determinants, eigenvectors and diagonalization.

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Prerequisites:

Text(s):
MATH 6308 (8599) - Advanced Linear Algebra I (online)
Graduate standing: MATH 2331 and a minimum of 3 semester hours transformations, eigenvalues and eigenvectors.
Linear Algebra | Edition: 4; Stephen H. Friedberg, Arnold J. Insel, Lawrence E. Spence;
ISBN: 9780130084514
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Prerequisites:
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Prerequisites:
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Prerequisites:

Text(s):

Description:
the course content is required

Syllabus

Text(s): No textbook required. Lecture notes provided.

Classical examples, Schwartz lemma, Riemann mapping theorem, complex hyperbolic geometry, Little and Picard theorems, Riemann surface theory and others.

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Prerequisites:
Text(s):

Description:

MATH 6361 (4424) - Applicable Analysis
Graduate standing. MATH 4332 or consent of instructor.
The instructor will provide lecture notes on the material. A reference text is L.D. Berkowitz, Convexity and Optimization in Rn, Wiley-Interscience 2002.

This course provides an introduction to the mathematical analysis of finite dimensional optimization problems. Topics to be studied include the existence of, and the extremality conditions that hold at, solutions of constrained and unconstrained optimaization problems. Elementary theory of convex sets, functions and constructions from convex analysis will be introduced and used. Concepts include subgradients, conjugate functions and some duality theory. Specific problems to be studied include energy and least squares methods for solving linear equations, important inequalities, eigenproblems and some nonlinear programming problems from applications.

MATH 6365 (12154) - Automatic Learning and Data Mining Graduate standing. MATH 3338 and MATH 3339.
The instructor will provide lecture notes on the material. A reference text is L.D. Berkowitz, Convexity and Optimization in Rn, Wiley-Interscience 2002.
Automatic learning and data mining cluster high-dimension inputs to predict their impact on decision outputs. Kernel based Clustering and Learning enable dictionary generation, pattern classification, non linear regression. Applications: shape recognition, genes expression analysis, etc.

MATH 6365 (13334) - Automatic Learning and Data Mining
Graduate standing. MATH 3338 and MATH 3339.
The instructor will provide lecture notes on the material. A reference text is L.D. Berkowitz, Convexity and Optimization in Rn, Wiley-Interscience 2002.
Automatic learning and data mining cluster high-dimension inputs to predict their impact on decision outputs. Kernel based Clustering and Learning enable dictionary generation, pattern classification, non linear regression. Applications: shape recognition, genes expression analysis, etc.

Prerequisites:

Text(s):

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Prerequisites:
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Prerequisites:

Text(s):

- D.P. Bertsekas; Dynamic Programming and Optimal Con- trol, Vol. I, 4th Edition. Athena Scientific, 2017, ISBN-10: 1-886529-43-4
- J.R. Birge and F.V. Louveaux; Introduction to Stochastic Programming. Springer, New York, 1997, ISBN: 0-387-98217-

Constrained and unconstrained finite dimensional nonlinear programming, optimization and Euler-Lagrange equations, duality, and numerical methods. Optimization in Hilbert spaces and variational problems. Euler-Lagrange equations and theory of the second variation. Application to integral and differential equations.

Additional Description: This course consists of two parts. The first part is concer- ned with an introduction to Stochastic Linear Programming (SLP) and Dynamic Programming (DP). As far as DP is concerned, the course focuses on the theory and the appli- cation of control problems for linear and nonlinear dynamic systems both in a deterministic and in a stochastic frame-work. Applications aim at decision problems in finance. In the second part, we deal with continuoustime systems and optimal control problems in function space with em- phasis on evolution equations.

## MATH 6371 (2943) - Numerical Analysis

Graduate standing:
Numerical Mathematics (Texts in Applied Mathematics), 2nd Ed., V.37, Springer, 2010. By A. Quarteroni, R. Sacco, F. Saleri. ISBN: 9783642071010
Ability to do computer assignments. Topics selected from numerical linear algebra, nonlinear equations and optimization, interpolation and approximation, numerical differentiation and integration, numerical solution of ordinary and partial differential equations.

Graduate standing. MATH 3334, MATH 3338 and MATH 4378.
Recommended Text: John A. Rice : Mathematical Statistics and Data Analysis, $3^{\text {rd }}$ editionBrooks / Cole, 2007. ISBN-13: 978-0-534-39942-9.

## Reference Texts:

-P. MuCullagh and J.A. Nelder: Generealized Linear Models, $2^{\text {nd }}$ ed. 1999 Chapman Hall/CRC. ISBN: 978-0412317606
-Raymond H. Myers, Douglas C. Montgomery, G. Geoffrey Vining, Timothy J. Robinson, Generalized Linear Models: with Applications in Engineering and the Sciences, $2^{\text {nd }}$ ed. Wiley, 2010. ISBN: 978-0-470-45463-3.

A survey of probability theory, probability models, and statistical inference. Includes basic probability theory, stochastic processes, parametric and nonparametric methods of statistics.

Instructor's Description: This course is designed for graduate students who have been exposed to basic probability and statistics and would like to learn more advanced statistical theory and techniques in modelling data of various types, including continuous, binary, counts and others. The selected topics will include basic probability distributions, likelihood function and parameter estimation, hypothesis testing, regression models for continuous and categorical response variables, variable selection methods, model selection, large sample theory, shrinkage models, ANOVA and some recent advances.

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Prerequisites:
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Prerequisites:

MATH 6385 (12153) - Continuous-Time Models in Finance
Graduate Standing. MATH 6384
Arbitrage Theory in Continuous Time, 3rd edition, by Tomas Bjork, Oxford University Press, 2009. (Primary)

Stochastic calculus, Brownian motion, change of measures, Martingale representation theorem, pricing financial derivatives whose underlying assets are equities, foreign exchanges, and fixed income securities, single-factor and multi-factor HJM models, and models involving jump diffusion and mean reversion.

Additional Description: The course is an introduction to continuous-time models in finance. We first cover tools for pricing contingency claims. They include stochastic calculus, Brownian motion, change of measures, and martingale representation theorem. We then apply these ideas in pricing financial derivatives whose underlying assets are equities, foreign exchanges, and fixed income securities. In addition, we will study models involving jump diffusion and mean reversion and the use of levy processes in finance.

MATH 6397 (13924) - Introduction to Sobolev Calculus and Sobolev Spaces Graduate standing.

There is no specific text for the course and the instructor will provide references for different parts of the material and some of his own notes. Three good references are specific chapters in the texts of:
K. Atkinson and W. Han, Theoretical Numerical Analysis, Texts in Applied Mathematics. Vol 39,

Text(s):

Description:
This course is an introduction to the theory of weak derivatives and Sobolev spaces as used currently in the analysis of partial differential equations and numerical analysis. The rules of calculus change substantially when derivatives are defined in a weak sense. Conditions for product or chain rules to hold are quite different from those in the classical theorems. Many functions with singularities and corners may have weak derivatives with nice properties and various formulae hold with extra terms or different interpretations. In many engineering models and physical problems the analysis using weak derivatives produces results that better describe the observed behavior.

The prerequisites for this course are classical multivariate calculus, and knowledge of Lebesgue and Borel measure on $\mathrm{R}^{N}$ and elementary Banach and Hilbert space theory as in graduate Real Analysis M6320 or equivalent. First weak derivatives of $L^{1}$ loc - functions on open subsets $\Omega \subset R^{N}$ will be defined. The definition generalizes the classical definition in some ways and is not a pointwise definition.

These definitions enable the statement and proof of weak versions of the basic theorems of both 1-dimensional and multivariate calculus. These include the product rule, the chain rule, the fundamental theorem of calculus and the Gauss-Green (divergence) theorem. Then some results that only hold for weak derivatives will be proved starting with results on commutativity of weak derivatives the derivatives of convolutions, of infs and sups of pairs of functions and the approximation of measurable functions using mollifiers.

Sobolev spaces such as $H^{1}(\Omega), W^{1, p}(\Omega), H(d i v, \Omega)$ and others will be defined and their properties described. These included completeness and imbedding theorems, the Poincar'e and Friedrich's inequalities and Rellich type theorems. Also some results about trace operators, spaces and equivalent inner products and norms.

If time permits, some results about $W^{1, p}\left(R^{N}\right)$ and the Sobolev and Morrey embedding theorems will be treated.

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Additional Description: The course is about time analysis with special emphases on financial and

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Prerequisites:
Text(s):

Prerequisites:

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,
energy data. The course covers ARIMA models, ARCH/GARCH models, nonlinear models, high frequency data analysis, parameter estimation for diffusion and related processes, multivariate time series, extreme value analysis, Copulas, Levy processes, and an introduction of Markov chain Monte Carlo Methods. We will use R for computing.

## MATH 7350 (13927) - Geometry Manifolds

Graduate standing.
MATH 7321 (13926) - Functional Analysis II
Graduate standing and MATH 7320 or instructor consent
Instructor Notes: Xeroxed set of lecture notes will be available. Recommended texts:Pedersen's "Analysis Now" or Conway's "A Course in Functional Analysis".

Catalog Description: This course is part of a two semester sequence covering the main results in functional analysis, including Hilbert spaces, Banach spaces, topological vector spaces such as distributions, and linear operators on these spaces.

Instructor's Description: This is a continuation of what was discussed in 7320. The second semester will mostly be a more technical development of the theory of linear operators on Hilbert space and related subjects. We will also cover topics which the students request as time permits.

Some of the main topics covered include: Banach algebras and the Gelfand transform. $\mathrm{C}^{*}$-algebras and the functional calculus for normal operators. The spectral theorem for normal operators. Trace, Hilbert-Schmidt, and Schatten classes. Unbounded operators (e.g. Extensions and closed operators, Cayley transform and the spectrum, the spectral theorem, Stone's theorem and the uncertainty principle). Student projects (such as the theory of von Neumann algebras, etc).

Instructor's Prerequisite: Math 4331 and familiarity with multivariable calculus (at least at the level of Math 2433-Calculus III) or consent of the instructor

Recommended: John M. Lee, Introduction to Smooth Manifolds, 2nd edition other relevant books will be placed on reserve in the library

This course describes the basic notions and constructions of differential geometry, and some of the more advanced results. It includes: manifolds, the inverse and implicit function theorems, submanifolds, partitions of unity; tangent bundles, vector fields, the Frobenius theorem, Lie derivatives, vector bundles; differential forms, tensors and tensor fieldson manifolds; exterior algebra, orientation, integration on manifolds, Stokes' theorem; Lie groups. A few additional topics might be also covered, depending on the interest of the audience.

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Prerequisites: Graduate standing:

Text(s):

Description:
MATH 7394 (13929) - Ergodic Theory \& Thermodynamic Formalism

The primary text is "An Introduction to Ergodic Theory", by Peter Walters. Another useful textbook is "Foundations of Ergodic Theory", by Marcelo Viana and Krerley Oliveira. I will also refer to "Equilibrium States and the Ergodic Theory of Anosov Diffeomorphisms", by Rufus Bowen, as well as various other primary sources from the research literature.

Ergodic theory is a central part of the theory of dynamical systems, studying the asymptotic statistical properties of systems evolving in time that preserve an invariant measure. Systems with chaotic behavior generally possess many invariant measures, and thermodynamic formalism borrows tools from statistical mechanics to select a distinguished measure that is physically relevant. The first part of the class will cover topics in classical ergodic theory, including Birkhoff's ergodic theorem, entropy, and the classification of Bernoulli automorphisms.

The remainder of the course will discuss thermodynamic formalism, including the description of Sinai-Ruelle-Bowen measure via absolute continuity, the description of Parry measure via a variational principle, and the connection between the two via the general theory of equilibrium states. Some time will be spent describing the different approaches to thermodynamic formalism and SRB measures in uniform hyperbolicity: Ruelle-Perron-Frobenius operators indirectly via symbolic dynamics or directly via anisotropic Banach spaces; specification and expansivity; and the geometric approach via averaged pushforwards. Time permitting, we will discuss connections to dimension theory and geometric measure theory, and will conclude with a discussion of the nonuniformly hyperbolic setting.

MATH 7396 (13927) - Multigrid Methods
Prerequisites:Graduate standing.
Text(s): TBA
Description: TBA

